

# CSE6488: Mobile Computing Systems

## An Efficient and Scalable Approach to CNN Queries in a Road Network

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## Introduction

- Example Queries on Figure 1
  - NN Query : Retrieve the 3 closest gas stations from a query point  $n_j$ .
  - CNN Query : Find the 2 closest gas stations from all points on the path  $P$  from  $n_1$  to  $n_6$  (i.e.,  $P = \{n_1, n_2, n_3, n_4, n_5, n_6\}$ ).

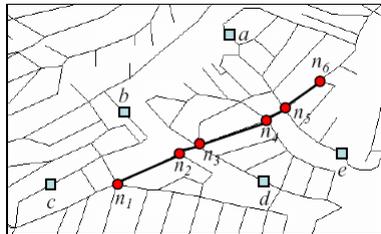


Fig 1. Example continuous search ( $a, b, c, d, e$  : gas stations)

## Related Work

- NN Queries in a Road Network
  - INE (Incremental Network Expansion)
    - Based on Dijkstra's algorithm
    - INE suffers from highly computational cost when objects of interest are sparsely distributed.
  - VN<sup>3</sup> (Voronoi-based Network NN Search)
    - VN<sup>3</sup> evaluates  $k$  NN queries using the Voronoi diagram
    - If the density of objects increases, VN<sup>3</sup> suffers from computational overhead of precalculating network Voronoi polygons

Figure 2: Sample network Voronoi diagram

- Unfortunately, the performance of existing approaches depends largely on the densities of the objects.

## Nearest Neighbor Search

- UNICONS (UNIque CONtinuous Search algorithms) for NN queries
  - It incorporates the precomputed NN lists in using Dijkstra's algorithm for NN queries
  - A node where three or more edges meet is called *an intersection point* and an intersection point which maintains precomputed NNs is called *a condensing point*.

Q : Which objects are the two NNs of  $q$ ?

A : The two NNs of  $q$  are  $a$  ( $4+26$ ) and  $b$  ( $4+49$ ).

Fig 3. Example NN query processing ( $n_1, n_2$  : condensing points)



## Two Basic Ideas of CNN Search

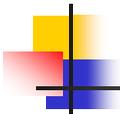
- The 1st basic idea
  - To perform a continuous search along a path  $P = \{n_i, n_{i+1}, \dots, n_j\}$ , it is sufficient to retrieve objects on the query path and to run a static query at each node  $n_k$  ( $i \leq k \leq j$ ).

$$\mathcal{R}_{path} = \mathcal{O}_{path} \cup \mathcal{R}_{n_i} \cup \mathcal{R}_{n_{i+1}} \cdots \cup \mathcal{R}_{n_j}$$

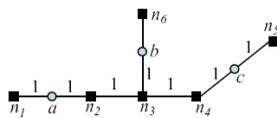
- The 2nd basic idea
  - The change in the network distance between a moving query point and a static object of interest can be expressed as *a piecewise linear equation*.



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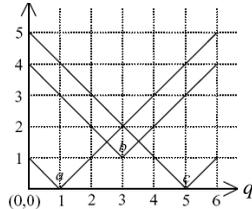


## Example of the two Basic Ideas



(a) path =  $\{n_1, n_2, n_3, n_4, n_5\}$   
 $d(q, obj)$

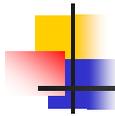
$$\mathcal{R}_{path} = \mathcal{O}_{path} \cup \mathcal{R}_{n_1} \cup \mathcal{R}_{n_2} \cup \mathcal{R}_{n_3} \cup \mathcal{R}_{n_4} \cup \mathcal{R}_{n_5}$$



(b)  $d(q, a) = |q - 1|$ ,  $d(q, b) = |q - 3| + 1$ ,  $d(q, c) = |q - 5|$

Fig 4.  $d(q, a)$ ,  $d(q, b)$ , and  $d(q, c)$

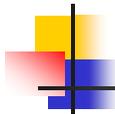
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## Sketch of CNN Search Algorithm

- Our CNN search algorithm based on **the divide and conquer method** proceeds with the following three steps:
  - [Step 1] Divide a query path into subpaths based on intersection points
  - [Step 2] Determine valid intervals for each subpath
  - [Step 3] Merge valid intervals of adjacent subpaths

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## Sketch of CNN Search Algorithm (cont'd)

- [Step 2] consists of the four sub-steps as follows:
  - [Step 2.1] Retrieve objects on the subpath
  - [Step 2.2] Issue two NN queries from the start and end points of the subpath
  - [Step 2.3] Remove some tuples obtained from Steps 2.1 and 2.2 using the *cover* relationship
  - [Step 2.4] Divide the subpath into valid intervals

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## CNN Search Algorithm for the subpath

- The result  $R$  of Steps 2.1 and 2.2 is the set of  $(obj, x, y)$  tuples
  - If  $obj$  (e.g.  $a$ ) is located on the subpath,  $x = d(s_{SP}, obj)$  and  $y = 0$ .
  - If  $obj$  (e.g.  $b$ ) is an object satisfying the query predicate at  $s_{SP}$ ,  $x = 0$  and  $y = d(s_{SP}, obj)$ .
  - If  $obj$  (e.g.  $c$ ) is an object satisfying the query predicate at  $e_{SP}$ ,  $x = L_{SP}$  and  $y = d(e_{SP}, obj)$

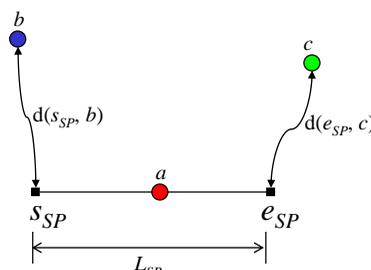
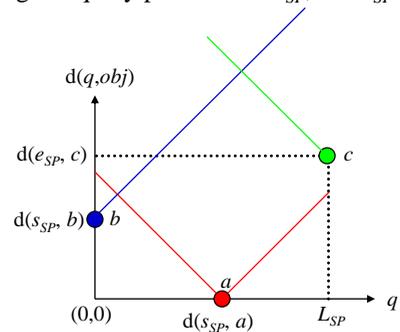



Fig 5. Plotting tuples on the chart  
( $q$  : location of the query point)

## The Cover Relationship

- The *cover* relationship
  - It is applied to tuples with the same object

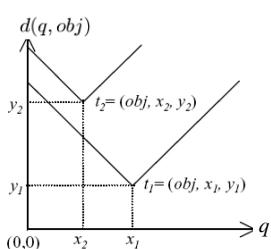


Fig 6.  $t_1$  covers  $t_2$  iff  $y_2 \geq |x_2 - x_1| + y_1$

- A tuple  $(obj, x, y)$  on the chart gives the network distance from  $q$  to  $obj$  as follows:  $d(q, obj) = |q - x| + y$



## Example of CNN Query Processing

- For static objects  $a$  to  $e$  on the road network of Figure 7, continuously display the two closest objects from any position on the query path  $P = \{n_3, n_5, n_7, n_8\}$ .

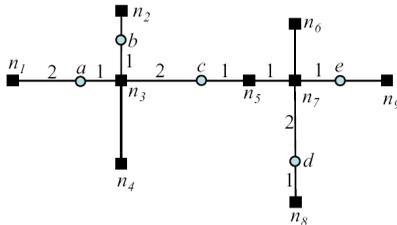


Fig 7. Example Road Network

[Step1] Divide a query path into subpaths  
 $: SP_1 = \{n_3, n_5, n_7\}$  and  $SP_2 = \{n_7, n_8\}$

[Step 2] Determine valid intervals for each subpath  
 : Detailed explanation is provided in the next slide

[Step 3] Merge valid intervals of adjacent subpaths

- [Step 2.1] Retrieve the objects on  $SP_1 = \{n_3, n_5, n_7\}$   
 $O_{SP_1} = \{(c, 2, 0)\}$
- [Step 2.2] Retrieve the qualifying objects on two end points  $s_{SP_1}$  and  $e_{SP_1}$   
 $S_{SP_1} = \{(a, 0, 1), (b, 0, 1)\}$  and  $E_{SP_1} = \{(e, 4, 1), (c, 4, 2)\}$   
 $\therefore R = O_{SP_1} \cup S_{SP_1} \cup E_{SP_1} = \{(c, 2, 0), (a, 0, 1), (b, 0, 1), (e, 4, 1), (c, 4, 2)\}$
- [Step 2.3] Remove redundant tuples using the *cover* relationship  
 $R = R - \{(c, 4, 2)\} \therefore R = \{(c, 2, 0), (a, 0, 1), (b, 0, 1), (e, 4, 1)\}$

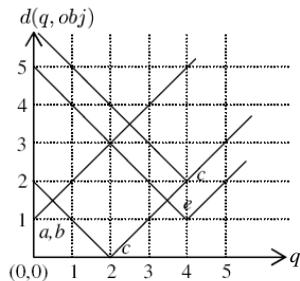


Fig 8. Plotting 5 tuples in  $R$  on the chart

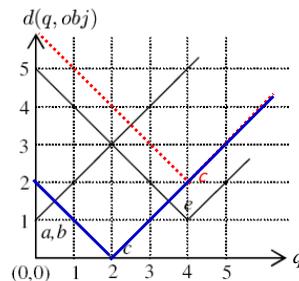


Fig 9. Filtering redundant tuples

## Example of CNN Query Processing (cont'd)

- [Step 2.4] Divide the subpath into valid intervals with a set of the same NNs

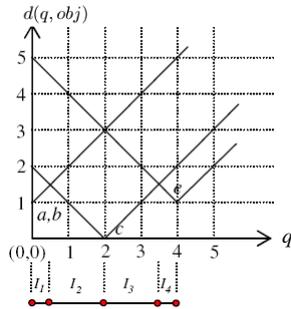


Fig 10. Dividing the query path into valid intervals

$I$	$R_I$
$I_1 = [0, \frac{1}{2}]$	$\{a, b\}$
$I_2 = [\frac{1}{2}, 2]$	$\{c, a\}$
$I_3 = [2, 3\frac{1}{2}]$	$\{c, e\}$
$I_4 = [3\frac{1}{2}, 4]$	$\{c, e\}$

(a) Initial Result

$I$	$R_I$
$I_1 = [0, \frac{1}{2}]$	$\{a, b\}$
$I_2 = [\frac{1}{2}, 2]$	$\{a, c\}$
$I'_3 = [2, 4]$	$\{c, e\}$

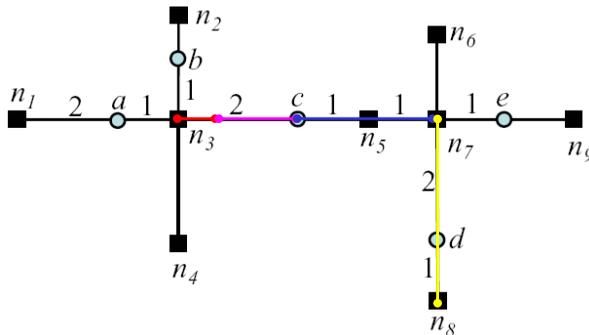
(b) Final Result

Fig 11. CNN Search result for  $SP_1 = \{n_3, n_5, n_7\}$

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## Example of CNN Query Processing (cont'd)

- In the same way, if we compute the CNN result for  $SP_2 = \{n_7, n_8\}$ , we can obtain  $R_{SP_2} = \{([4, 7], \{d, e\})\}$
  - [Step 3] Merge  $R_{SP_1}$  and  $R_{SP_2}$  for  $SP_1$  and  $SP_2$ , respectively, in order to obtain the final query result  $R_p$
- $\therefore R_p = R_{SP_1} \cup R_{SP_2} = \{([0, \frac{1}{2}], \{a, b\}), ([\frac{1}{2}, 2], \{a, c\}), ([2, 4], \{c, e\}), ([4, 7], \{d, e\})\}$



Interval	Results
$[0, \frac{1}{2}]$	$\{a, b\}$
$[\frac{1}{2}, 2]$	$\{a, c\}$
$[2, 4]$	$\{c, e\}$
$[4, 7]$	$\{d, e\}$

Fig 12. CNN Search result for  $P = \{n_3, n_5, n_7, n_8\}$

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